

# Fundamentals of E.E. Final Exam, 2019

Fundamental of Electrical Engineering (Final Examination)

## Part I

1. Define the following terms: (05pts)

- i. Resonance
- ii. Power factor correction
- iii. Angular velocity
- iv. Phase difference
- v. Peak to peak value

15

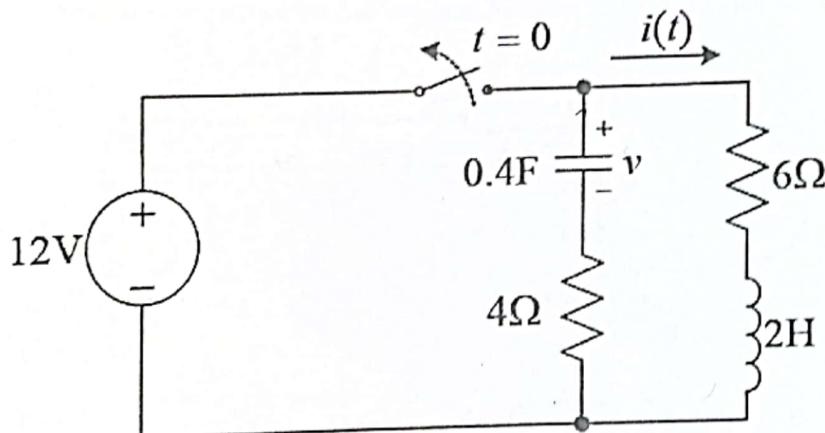
## Part II

1. For the circuit shown in Fig.1, find (06pts)

- i.  $i(0^+)$  and  $v(0^+)$
- ii.  $di(0^+)/dt$  and  $dv(0^+)/dt$
- iii.  $i(\infty)$  and  $v(\infty)$

12V

15



24

Fig.1.

2. An alternating current 'i' is given by;  $i(t) = 141.4 \sin(314t)$ . Find (05pts)

- i. the maximum value
- ii. frequency
- iii. time period
- iv. the instantaneous value when  $t$  is 3ms.
- v. Phase angle with respect to  $i(0)$

6

$$\frac{1}{2} \cdot 141.4 \cdot \frac{1}{2\pi f} = 82.8$$

141.4

82.8

3ms

14

Fundamental of Electrical Engineering (Final Examination)

3. A  $5\Omega$  resistor,  $60\text{mH}$  inductor and  $10\mu\text{F}$  capacitor are connected in parallel to a  $300\text{V}$ ,  $50\text{Hz}$  AC supply. Calculate (8pts)

- the current flowing,  $I_{\text{an}}$
- the phase difference between the supply voltage and current,
- the voltage across the circuit elements, ✓
- draw the phasor and admittance diagram.

4. An R-L-C series Ac circuit consists of resistance  $1000\Omega$ , Q-factor of the circuit **10** and the bandwidth of  $1000\text{Hz}$ . If a voltage of  $100\text{V}$  is applied across the combination. Find

- the resonant frequency
- inductance of the circuit
- capacitance of the circuit
- the half power frequencies

$$\begin{aligned} p(\omega_0) &= \frac{V_m^2}{2R} \\ p(\omega_{-1}) &= \frac{V_m^2}{4R} \end{aligned}$$

5. A  $4\text{kVAR}$ ,  $300\text{-V}$  (peak value),  $50\text{-Hz}$  load has a power factor of  $0.95$  lagging. What value of capacitance have to be removed from the load, where the power factor falls to  $0.8$ ? (8pts)

$$\frac{2100}{\sqrt{2}}$$

\*\*\*\*\*

$$Q = \frac{\omega_0 - \omega}{\omega_0}$$

$$Q = \frac{\omega_0}{\omega}$$

$$2i_f = + \text{ (lag)} - \text{ (lead)}$$

$$Q \rightarrow \text{pf.}$$

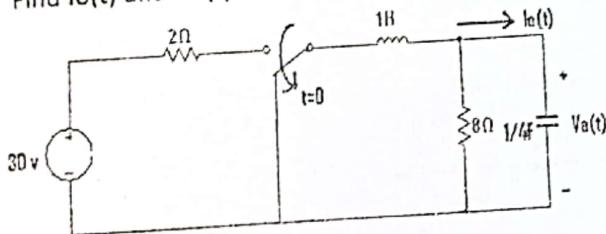
$$V_A = I_R$$

$$B_2$$

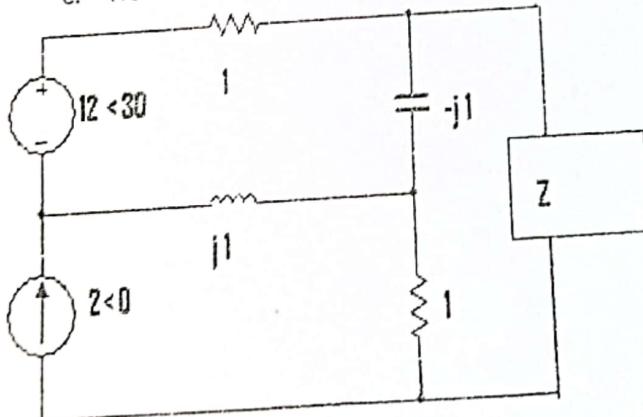
$$Q = \frac{V_0}{6.27 kV}$$

$$V_B = I_T$$

1. A  $4\Omega$  resistor,  $125mH$  inductor and  $10\mu F$  capacitor are connected in series to a  $230V$ ,  $50Hz$  AC supply. Calculate
- The current flowing, (2pts)
  - The phase difference between the supply voltage and current, (2pts) (3pts)
  - The voltage across each circuit element,.....(4pts)
  - Draw the phasor and impedance diagram.....(4pts)
2. When connected to a  $230 V$  (peak),  $60-Hz$  power line, a load absorbs  $10 \text{ kW}$  at a lagging power factor of  $0.8$ . Find the value of capacitance necessary to raise the pf to  $0.9$ . (6pt)
3. A  $240-V_{\text{peak}}$   $60\text{Hz}$  supply serves a load that is  $20\text{kW}$ ,  $15\text{kvar}(\text{capacitive})$  and  $20\text{kVAR}(\text{inductive})$ .find:
- Apparent power .....(3pts)
  - The current drawn from the supply.....(3pts)
  - The kVAR rating and capacitance required to improve the power factor to  $0.95$  lagging..(5pts) (7pts)
4. Find  $i_o(t)$  and  $v_o(t)$  for  $t > 0$ .....(7pts)



- 5.
- What must be the value of  $Z$  for maximum power transfer to it?.....(4pts)
  - What is amount of the average power absorbed by the impedance?.....(4pts)
  - How much is the maximum power?.....(2pts)



1. A  $4\Omega$  resistor,  $125\text{mH}$  inductor and  $10\mu\text{F}$  capacitor are connected in series to a  $230\text{V}$ ,  $50\text{Hz}$  AC supply. Calculate

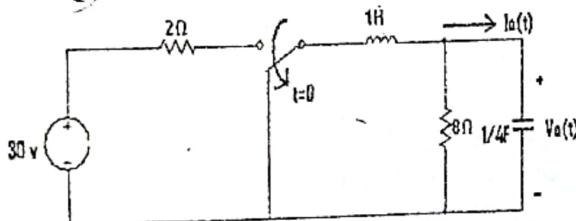
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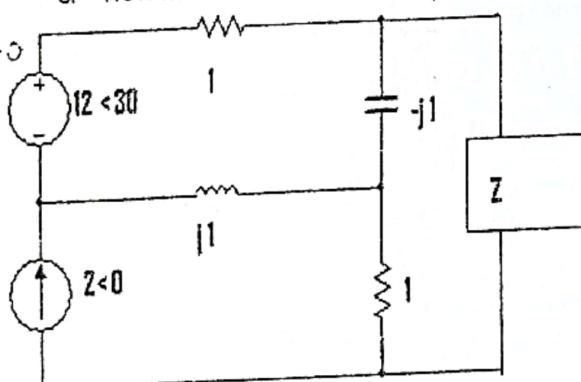
- Apparent power .....(3pts)
- The current drawn from the supply.....(3pts)
- The kVAR rating and capacitance required to improve the power factor to  $0.9$  lagging..(5pts)

4. Find  $\phi(t)$  and  $V_o(t)$  for  $t > 0$ .....(7pts)



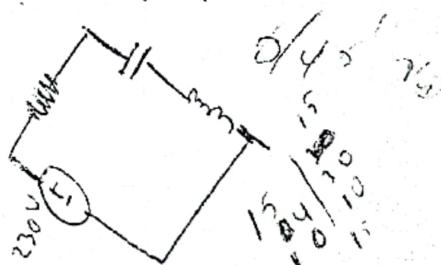
$$\omega = 2\pi f = 2 \times 60 \times 2\pi \text{ rad/s}$$

- What must be the value of  $Z$  for maximum power transfer to it?.....(4pts)
- What is amount of the average power absorbed by the impedance?.....(4pts)
- How much is the maximum power?.....(2pts)



$$R_L = -\frac{(V_o)(R_3)}{Z_L}$$

$$A_1 = \frac{V_o}{V_s} = \frac{R_1}{R_1 + R_3} = \frac{1}{1 + 5} = \frac{1}{6}$$



$$Z = \sqrt{R^2 + X^2} = \sqrt{5^2 + 1^2} = \sqrt{26}$$

3

## Fundamental of electrical engineering final exam (40%)

1. A certain load has voltage and current variation of a form given by:

$$v(t) = 12\sin(50t + 30^\circ) \text{ V and}$$

$$i(t) = 5\sin(50t - 45^\circ) \text{ A} \quad V(t) = 12\sin(50t + 30^\circ)$$

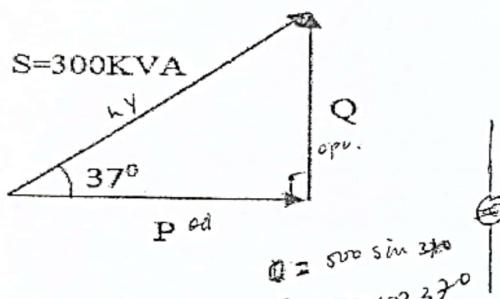
Find:

- The phase relation between the current and voltage.
- The instantaneous power at  $t=1 \text{ sec}$ .
- The average power consumed by the load.

$$\begin{aligned} i(t) &= 5 \angle -45^\circ \\ v(t) &= 12 \angle 30^\circ \\ v(t) &= 12 \angle 30^\circ \quad i(t) \text{ by } 75^\circ \text{ or} \\ v(t) &= 12 \angle 30^\circ \quad i(t) \text{ lags } v(t) \text{ by } 75^\circ \\ P &= Vi = 12 \times 5 = 60 \end{aligned}$$

2. A 600V, 300KVA small electrical utility supplies a factory with the power triangle shown in the figure here under.

(6 points)

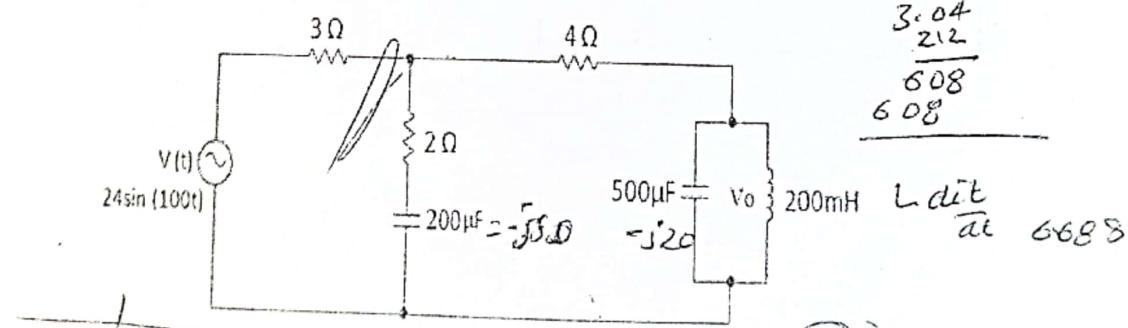


Determine:

- Total reactive power and real (true) power.
- Total current.

3. Referring to figure 1 determine:  $1.2 \text{ V.U.m}$  (12 points)

- Total impedance seen by the source ( $Z_T$ ).  $12 \sin(50t + 30^\circ) \text{ V}$
- Total current supplied by the source ( $I_T$ ).  $\frac{1}{j} I_T =$
- The output voltage ( $V_o$ ).
- Draw the phasor diagram and impedance diagram.



$$200 \times 10^3 \times 10^{-6}$$

$$= 2 \times 10^{-2} = \frac{100}{2} = 50$$

$$-j30+4$$

$$\begin{aligned} i(t) &= 3 \angle 30^\circ \\ V(t) &= 12 \cos 30^\circ \\ &= 10.4 \\ &= 10.4 \angle 30^\circ \end{aligned}$$

(6 points)  $\rightarrow 13$

$2.33$

$$V(t) = 12 \cos 30^\circ$$

$$= 10.4$$

$$\angle 30^\circ$$

$$= 10.4 \angle 30^\circ$$

4. Referring to fig 2 Determine:

(6 points)

- The value of  $Z_L$  to transfer maximum power to the load.
- Maximum power transfer to the load under this condition.

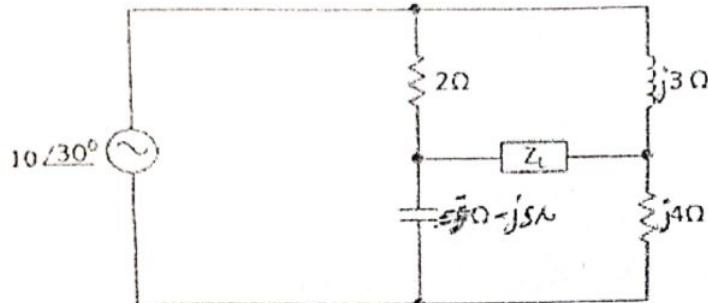


Fig. 2

5. Referring to figure 3 determine  $V_C(t)$  for  $t > 0$  and draw the response graph (use the appropriate method). (10 points)

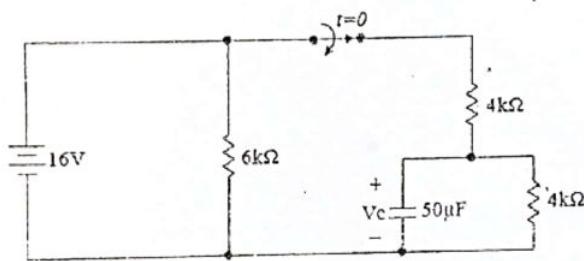


Fig.3

$R_{Th}$   $T_C$

$$\begin{aligned} R_{Th} &= 2 \text{ k}\Omega \\ T_C &= R_{Th} L_C \\ &= 2 \times 10^3 \times 70 \times 10^{-6} \\ &= 140 \text{ ms} \\ &\approx 0.14 \text{ s} \end{aligned}$$

### Bonus question

6. Referring to figure 4 find  $i(t)$  for  $t > 0$

(Step) 6

(5 points)  
from previous answer

$$\begin{aligned} K_1 &\sim V_C(0^-) = 2 \text{ V} \\ K_2 &\sim V_C(0^+) = V_{CC} \\ &\sim 8 \text{ V} \\ V_C(t) &\sim -t/2 + 8 \text{ e}^{-2t} \end{aligned}$$

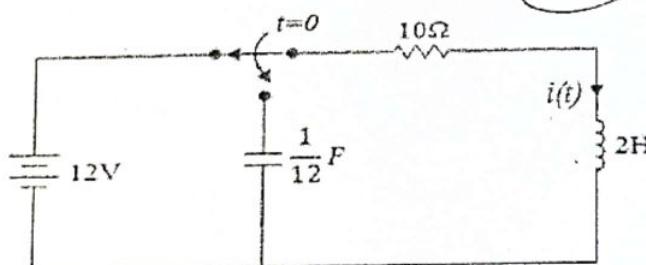


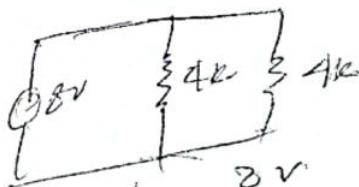
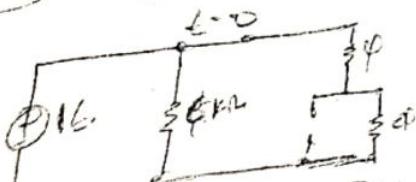
Fig 4

(Step 3)

$V(t)$  for  $t > 0$

Step ①  
 $V_C(t) = K_1 + K_2 e^{-2t}$

at  $t = 0$  - cut steady state  $t \rightarrow \infty$



$$\begin{aligned} K_1 &\sim V_C(0^-) = 2 \text{ V} \\ \text{Step ④} &\quad V_C(0^+) = 0 \end{aligned}$$

(5)